MATHCOUNTS®

2020 Chapter Competition **Sprint Round** Problems 1-30

HONOR PLEDGE

I pledge to uphold the highest principles of honesty and integrity as a Mathlete[®]. I will neither give nor accept unauthorized assistance of any kind. I will not copy another's work and submit it as my own. I understand that any competitor found to be in violation of this honor pledge is subject to disqualification.

Signature _____ Date _____

Printed Name

School _____

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO DO SO.

This section of the competition consists of 30 problems. You will have 40 minutes to complete all the problems. You are not allowed to use calculators, books or other aids during this round. If you are wearing a calculator wrist watch, please give it to your proctor now. Calculations may be done on scratch paper. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the left-hand column of the competition booklet. If you complete the problems before time is called, use the remaining time to check your answers.

In each written round of the competition, the required unit for the answer is included in the answer blank. The plural form of the unit is always used, even if the answer appears to require the singular form of the unit. The unit provided in the answer blank is the only form of the answer that will be accepted.

Total Correct	Scorer's Initials

Raytheon 2020 MATHCOUNTS **National Competition Sponsor**

TITLE SPONSORS **Raytheon Company**

NATIONAL SPONSORS

Northrop Grumman Foundation U.S. Department of Defense STEM National Society of Professional Engineers 3Mgives Texas Instruments Incorporated **CNA** Insurance Art of Problem Solving NextThought

FOUNDING SPONSORS: National Society of Professional Engineers, National Council of Teachers of Mathematics and CNA Insurance

Copyright MATHCOUNTS, Inc. 2019. All rights reserved.

0

1

2

3

4

5

6

7

8

9



Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Sprint Round

6. <u>furlon</u>	If 3 miles equal 1 league and 1 league equals 24 furlongs, how many furlongs are equal to 1 mile?
7degre	In quadrilateral ABCD, $m \angle A = 119^\circ$, $m \angle B = 89^\circ$ and $m \angle C = 49^\circ$. What is the degree measure of $\angle D$? B
8	If the first four terms of a geometric sequence are 2, 4, 8, 16 what is the fifth term of this sequence?
9sid	Gladys draws two polygons. Her second polygon has two fewer than twice as many sides as her first polygon. If Gladys' first polygon is a triangle, how many sides does her second polygon have?
10. <u>\$</u>	Lolli's Candy Store sells fruit-flavored candy rope, priced by length, at \$4.00 per meter. At this rate, how much will it cost to buy 50 cm of candy rope?

Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Sprint Round

11	Misko had an average score of 70 for her first three rounds of golf. If her scores for the first two rounds were 68 and 72, what was her score for the third round?
12. <u>cm²</u>	In the figure shown, the shaded inner square has area 36 cm ² , and each of its vertices intersects the midpoint of a side of the outer square. What is the area of the outer square?
13. <u>meters</u>	Rafa and Sascha played a long 320-point tennis match. If Rafa ran an average of 12.7 meters per point and Sascha ran an average of 11.8 meters per point, how many more meters did Rafa run over the course of the match?
14. <u>units²</u>	The length and width of a rectangle add up to 16 units, and the length is three times the width. What is the area of the rectangle?
15	What is the value of $\sqrt{5 \cdot 6 \cdot 10 \cdot 12}$?
	Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Sprint Round







MATHCOUNTS[®]

2020 ■ Chapter Competition ■ Target Round Problems 1 & 2

Name _____

School _

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO DO SO.

This section of the competition consists of eight problems, which will be presented in pairs. Work on one pair of problems will be completed and answers will be collected before the next pair is distributed. The time limit for each pair of problems is six minutes. The first pair of problems is on the other side of this sheet. When told to do so, turn the page over and begin working. This round assumes the use of calculators, and calculations also may be done on scratch paper, but no other aids are allowed. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the left-hand column of the problem sheets. If you complete the problems before time is called, use the time remaining to check your answers.

Problem 1	Problem 2	Scorer's Initials

TITLE SPONSORS Raytheon Company

NATIONAL SPONSORS

Northrop Grumman Foundation U.S. Department of Defense STEM National Society of Professional Engineers 3Mgives Texas Instruments Incorporated CNA Insurance Art of Problem Solving NextThought



National Competition Sponsor

FOUNDING SPONSORS: National Society of Professional Engineers, National Council of Teachers of Mathematics and CNA Insurance

Copyright MATHCOUNTS, Inc. 2019. All rights reserved.

0

1

2

3

4

5

6

7

8

9



x

Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Target Round

Problems 3 & 4
chool

TITLE SPONSORS **Raytheon Company**

NATIONAL SPONSORS

Northrop Grumman Foundation U.S. Department of Defense STEM National Society of Professional Engineers 3Mgives Texas Instruments Incorporated **CNA** Insurance Art of Problem Solving NextThought



2020 MATHCOUNTS National Competition Sponsor

FOUNDING SPONSORS: National Society of Professional Engineers, National Council of Teachers of Mathematics and CNA Insurance



	2020 ■ Chapter Competition Target Round Problems 5 & 6	
lame		
chool		
JO NOT BEG	AIN UNTIL YOU ARE INSTRU	CIED IO DO S

TITLE SPONSORS

Raytheon Company

NATIONAL SPONSORS

Northrop Grumman Foundation U.S. Department of Defense STEM National Society of Professional Engineers 3Mgives Texas Instruments Incorporated CNA Insurance Art of Problem Solving NextThought



2020 MATHCOUNTS National Competition Sponsor

FOUNDING SPONSORS: National Society of Professional Engineers, National Council of Teachers of Mathematics and CNA Insurance

Addi, Subbi, Multi and Divi, are given two distinct nonzero numbers. Addi adds the two numbers. Subbi subtracts the lesser number from the greater. Multi multiplies the two numbers. Divi divides the greater number by the lesser. If the results obtained by Addi, Multi and Divi are the same, what is Subbi's result? Express your answer as a common fraction.

6.

 cm^2

5.

Three geometrically similar George Washington profiles are attached to the sides of a right triangle with leg lengths of 6.2 cm and 9.3 cm. The height of each profile is equal to the length of the side to which it is attached. If the largest profile has an area of 25 cm², what is the area of the smallest profile, shown here shaded? Express your answer as a common fraction.



Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Target Round

ame
Chool

Problem 7	Problem 8	Scorer's Initials

TITLE SPONSORS Raytheon Company

NATIONAL SPONSORS

Northrop Grumman Foundation U.S. Department of Defense STEM National Society of Professional Engineers 3Mgives Texas Instruments Incorporated CNA Insurance Art of Problem Solving NextThought



2020 MATHCOUNTS National Competition Sponsor

FOUNDING SPONSORS: National Society of Professional Engineers, National Council of Teachers of Mathematics and CNA Insurance

The polygon shown is a dodecagon with six diagonals, each of length 10 meters and intersecting at its center. This polygon has 8 sides of length $\sqrt{10}$ meters each and 4 sides of length $\sqrt{2}$ meters each. What is the area of this dodecagon?



8. percent

The bar graphs shown give the probability for Team North and Team South to each score a specified integer number of goals per period. Based on this data and assuming the numbers of goals scored by each team are independent of each other, what is the probability that Team South will be in the lead at the end of the first period? Express your answer as a percent to the nearest whole number.



7.

 m^2

MATHCOUNTS[®]

2020 ■ Chapter Competition ■ Team Round Problems 1–10

School _____

Team Members

_____, Captain

0

1

2

3

4

5

6

7

8

9

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO DO SO.

This section of the competition consists of 10 problems which the team has 20 minutes to complete. Team members may work together in any way to solve the problems. Team members may talk to each other during this section of the competition. This round assumes the use of calculators, and calculations also may be done on scratch paper, but no other aids are allowed. All answers must be complete, legible and simplified to lowest terms. The team captain must record the team's official answers on his/her own competition booklet, which is the only booklet that will be scored. If the team completes the problems before time is called, use the remaining time to check your answers.

Total Correct	Scorer's Initials

TITLE SPONSORS Raytheon Company

NATIONAL SPONSORS

Northrop Grumman Foundation U.S. Department of Defense STEM National Society of Professional Engineers 3Mgives Texas Instruments Incorporated CNA Insurance Art of Problem Solving NextThought



FOUNDING SPONSORS: National Society of Professional Engineers, National Council of Teachers of Mathematics and CNA Insurance

Jack goes on a road trip across the Southwest, during which he buys fuel in several cities. The table shows the amounts and prices of the fuel Jack bought in

each city. What is the greatest amount Jack spent on fuel in any of these cities?

Road Trip Fuel Purchases

Сіту	GALLONS	PRICE (per gallon)
Las Cruces, NM	10.44	2.47
Tucson, AZ	10.01	2.41
Flagstaff, AZ	10.39	2.65
Las Vegas, NV	9.16	2.62



1. \$

3.

4.

For the 5×5 array shown, Chad fills in each empty cell with a positive integer so that any two cells that are vertically or horizontally adjacent contain numbers that differ by exactly 1. What is the greatest number that can appear in any of these cells?

times Marko's heart beats 72 times per minute during normal activity. It beats 65 times per minute during sleep, and 118 times per minute when Marko is exercising. During a 24-hour period, Marko slept from 10:00 p.m. until 5:00 a.m. and then exercised from 5:30 a.m. to 7:30 a.m. For the remaining time he had normal activity. During that 24-hour period, how many times did Marko's heart beat?

years Kepler's third law of planetary motion states that the square of the amount of time it takes for a planet to orbit the Sun is proportional to the cube of the planet's greatest distance from the Sun. Based on this and the data for Mars, Jupiter, Uranus and Neptune included in the table shown, how many Earth years does it take for Neptune to orbit the Sun? Express your answer to the nearest whole number.

Planet	GREATEST DISTANCE (kilometers to Sun)	ORBIT TIME (Earth years)
Mars	2.28×10^{8}	1.882
Jupiter	7.78×10^{8}	11.86
Uranus	2.87×10^{9}	84.01
Neptune	4.50×10^{9}	?

Sun Distances and Orbit Times

An ordered triple (a, b, c) is randomly chosen from the set of all ordered triples for which a, b and c are nonnegative integers that satisfy a + b + c = 22. What is the probability that a < b < c? Express your answer as a common fraction.

Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Team Round

5.

6. <u>sequences</u>	Lincoln stands at vertex A of hexagon ABCDEF and rolls a die three times. For each roll, if the number rolled is even, he moves clockwise that number of vertices. If the number rolled is odd, he moves counter-clockwise that number of vertices. How many different sequences of three rolls will result in Lincoln ending at vertex A?
7	An abundant number is a positive integer n for which the sum of the positive integer factors of n is greater than $2n$. What is the sum of all the abundant numbers that are less than 60?
8. lengths	Suppose 7 points lie in a plane, and a line segment is drawn connecting each pair of points, forming a total of 21 line segments. What is the minimum number of distinct lengths among the 21 line segments?
9	A standard 52-card deck of playing cards has thirteen ranks in each of four suits. If five cards are randomly selected from the deck, without replacement, what is the probability that they are all the same suit? Express your answer as a decimal to the nearest thousandth.
10. <u>units²</u>	Let <i>R</i> be the set of all points (x, y) satisfying $x^2 + y^2 \le 100$. What is the least possible area of a right triangle with three integer side lengths that cannot fit inside <i>R</i> ?
	Copyright MATHCOUNTS, Inc. 2019. All rights reserved. 2020 Chapter Team Round